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# Automated Repair of Process Models Using Non-Local Constraints

Anna Kalenkova\*, Josep Carmona\*\*, Artem Polyvyanyy\*, Marcello La Rosa\*

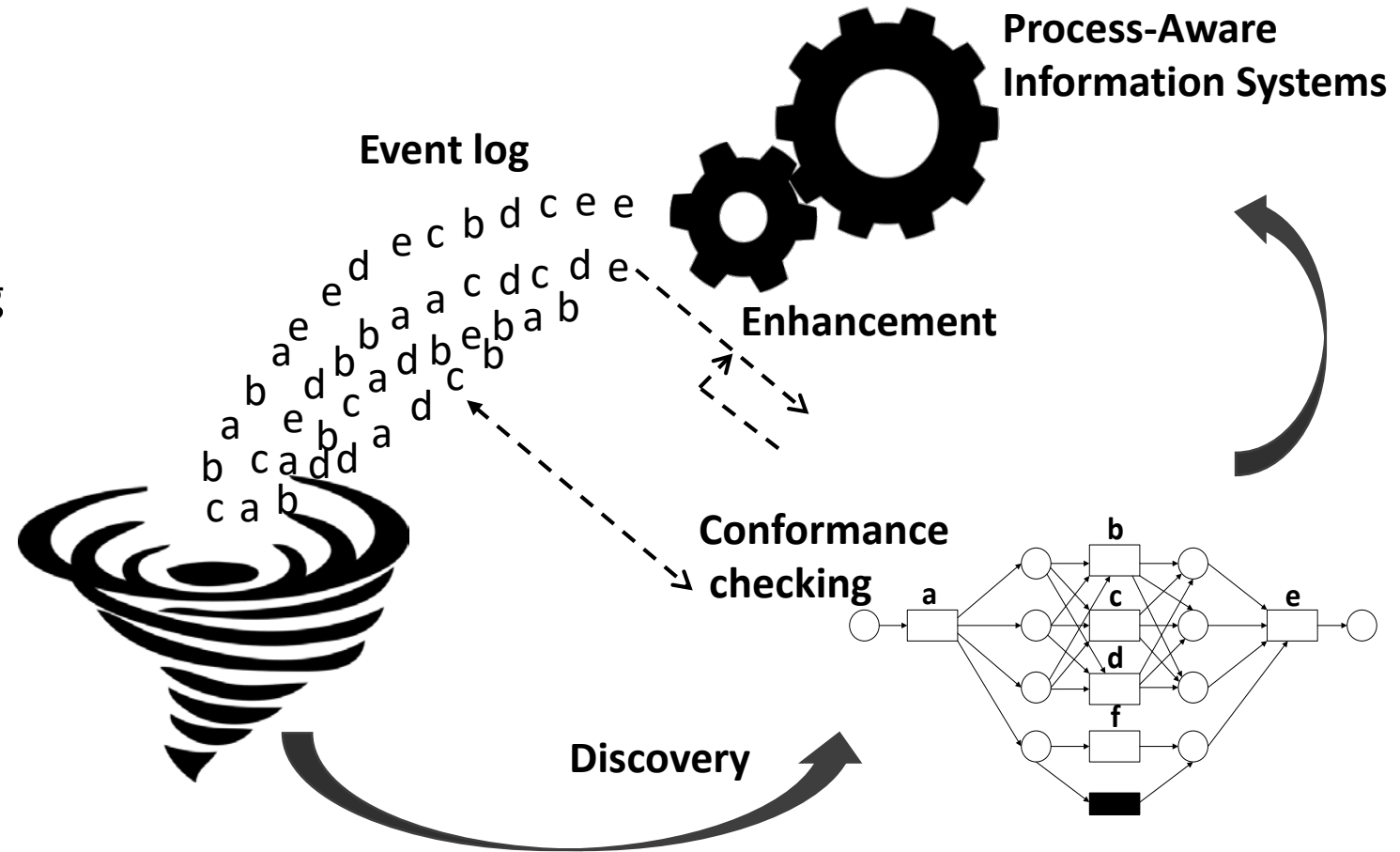
\* The University of Melbourne

\*\* Polytechnic University of Catalonia



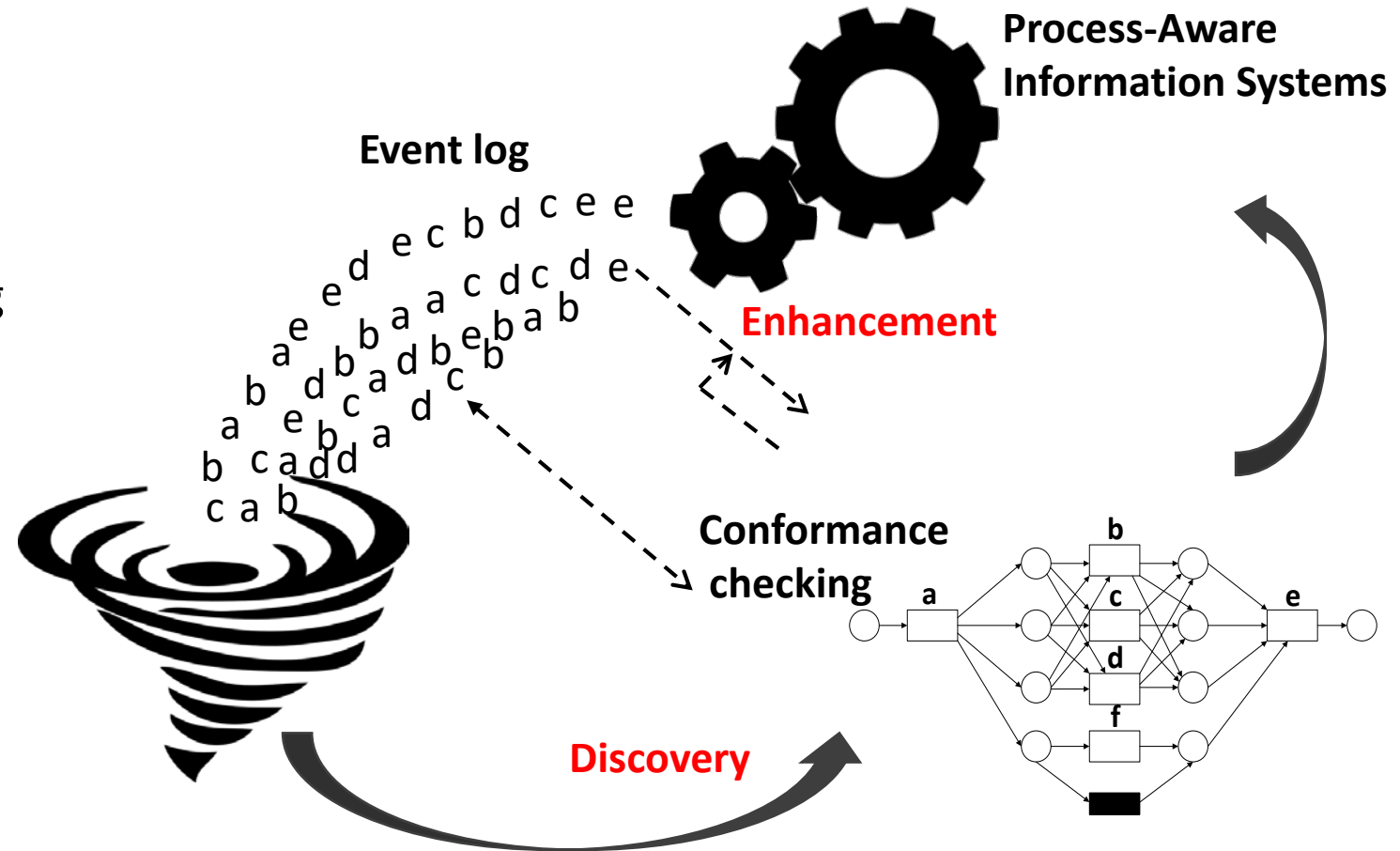
# Process mining

- Discovery
- Conformance checking
- Enhancement



# Process mining

- **Discovery**
- Conformance checking
- **Enhancement**



# Discovery. Event log

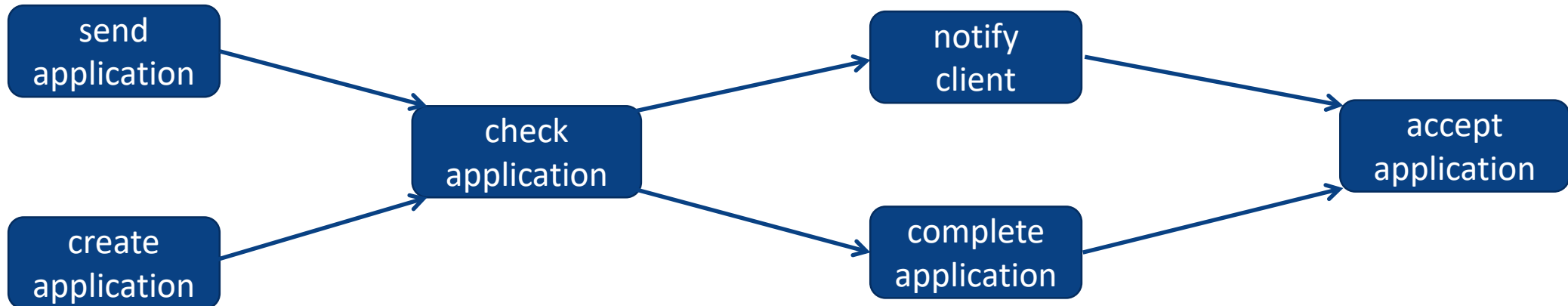
Case ID	Activity name	Timestamp
1	<i>send application</i>	2019-10-28T10:02:30
2	<i>create application</i>	2019-10-28T10:03:17
1	<i>check application</i>	2019-10-28T10:03:58
1	<i>notify client</i>	2019-10-28T10:04:20
1	<i>accept application</i>	2019-10-28T10:04:25
2	<i>check application</i>	2019-10-28T14:32:51
2	<i>complete application</i>	2019-10-29T09:45:13
2	<i>accept application</i>	2019-10-29T09:50:45



$$L = \{ \langle \textit{send application}, \textit{check application}, \textit{notify client}, \textit{accept application} \rangle, \langle \textit{create application}, \textit{check application}, \textit{complete application}, \textit{accept application} \rangle \}.$$

# Discovery. Directly-Follows Graphs (DFGs)

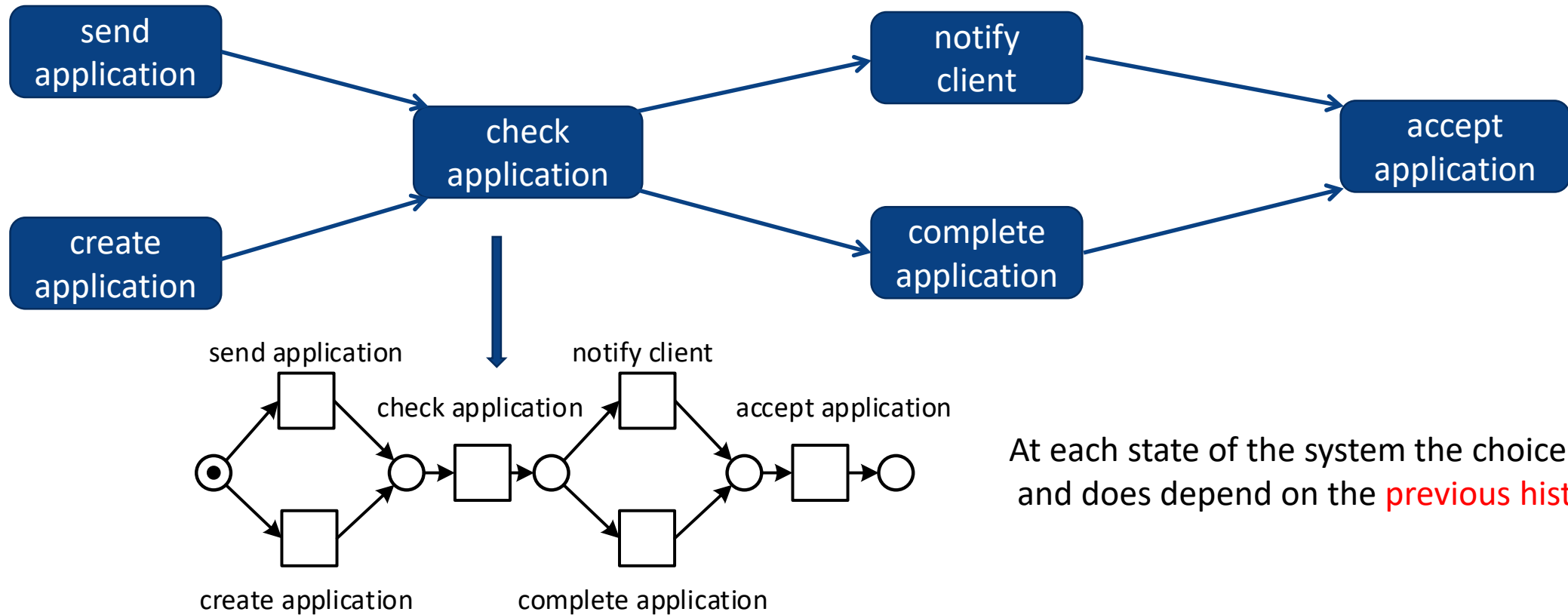
$L = \{ \langle \textit{send application}, \textit{check application}, \textit{notify client}, \textit{accept application} \rangle, \langle \textit{create application}, \textit{check application}, \textit{complete application}, \textit{accept application} \rangle \}$ .



DFGs are used as a **final** process representation in **commercial process mining tools**. As well as an **intermediate** process representation within scalable process mining algorithms, e.g., Inductive miner and Split miner that discover **free-choice nets** such as BPMN models.



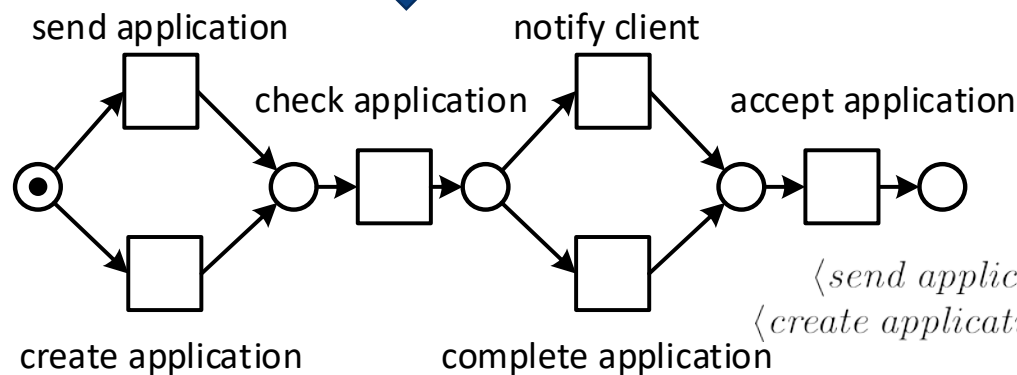
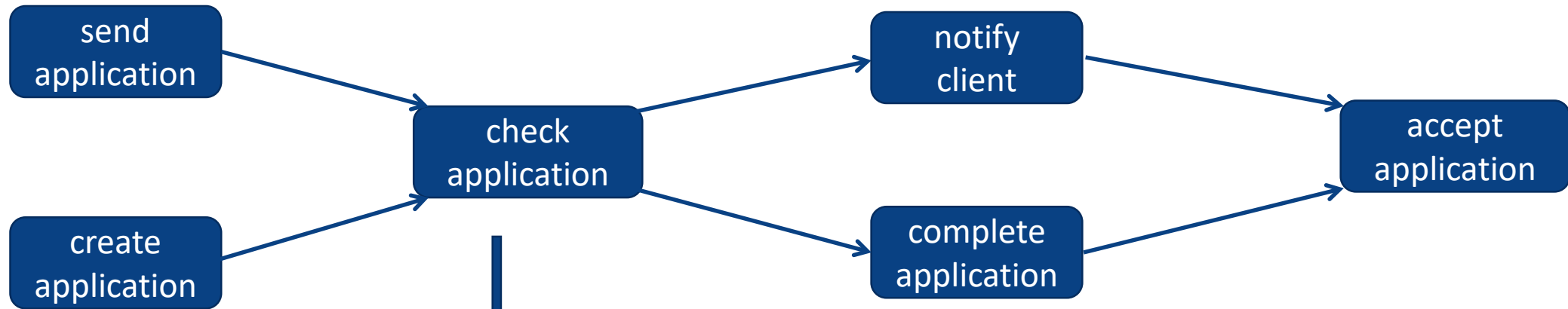
# Discovery. Directly-Follows Graphs (DFGs)



At each state of the system the choice is **free** and does depend on the **previous history**.



# Discovery. Directly-Follows Graphs (DFGs)

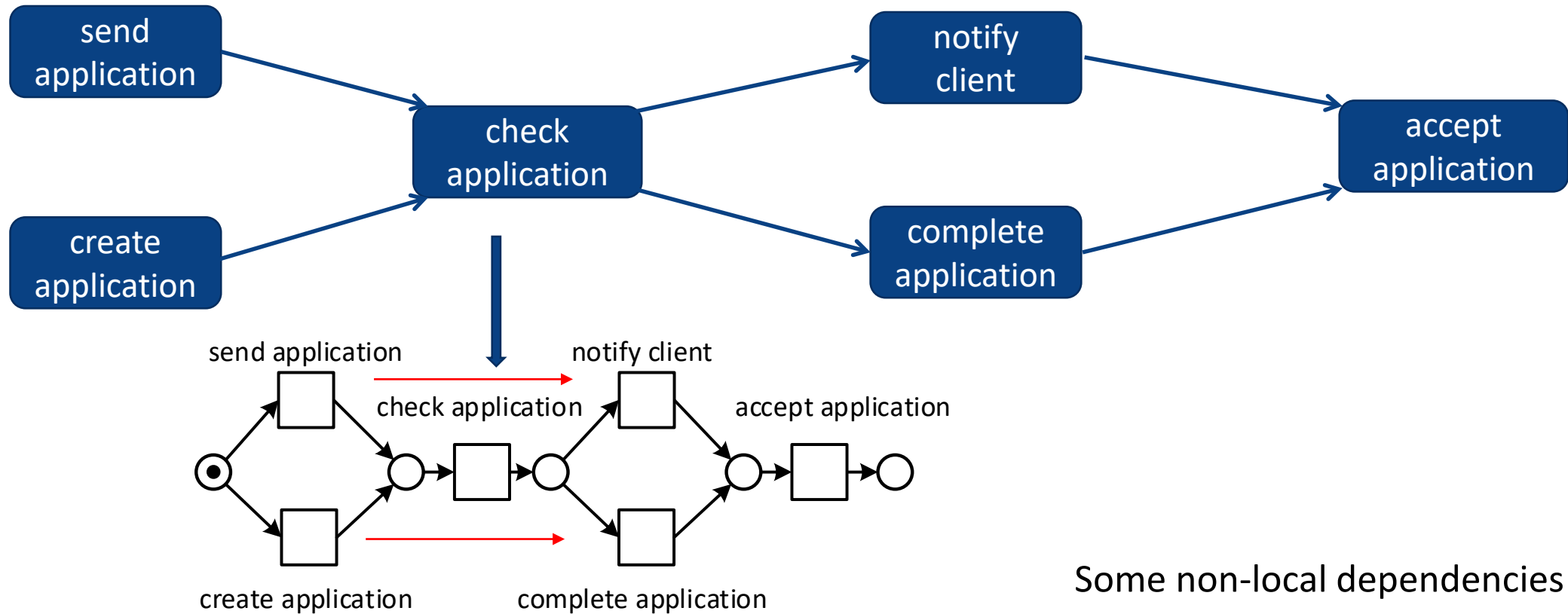


Two additional traces:

$\langle \text{send application}, \text{check application}, \text{complete application}, \text{accept application} \rangle$ ,  
 $\langle \text{create application}, \text{check application}, \text{notify client}, \text{accept application} \rangle$ .



# Discovery. Directly-Follows Graphs (DFGs)

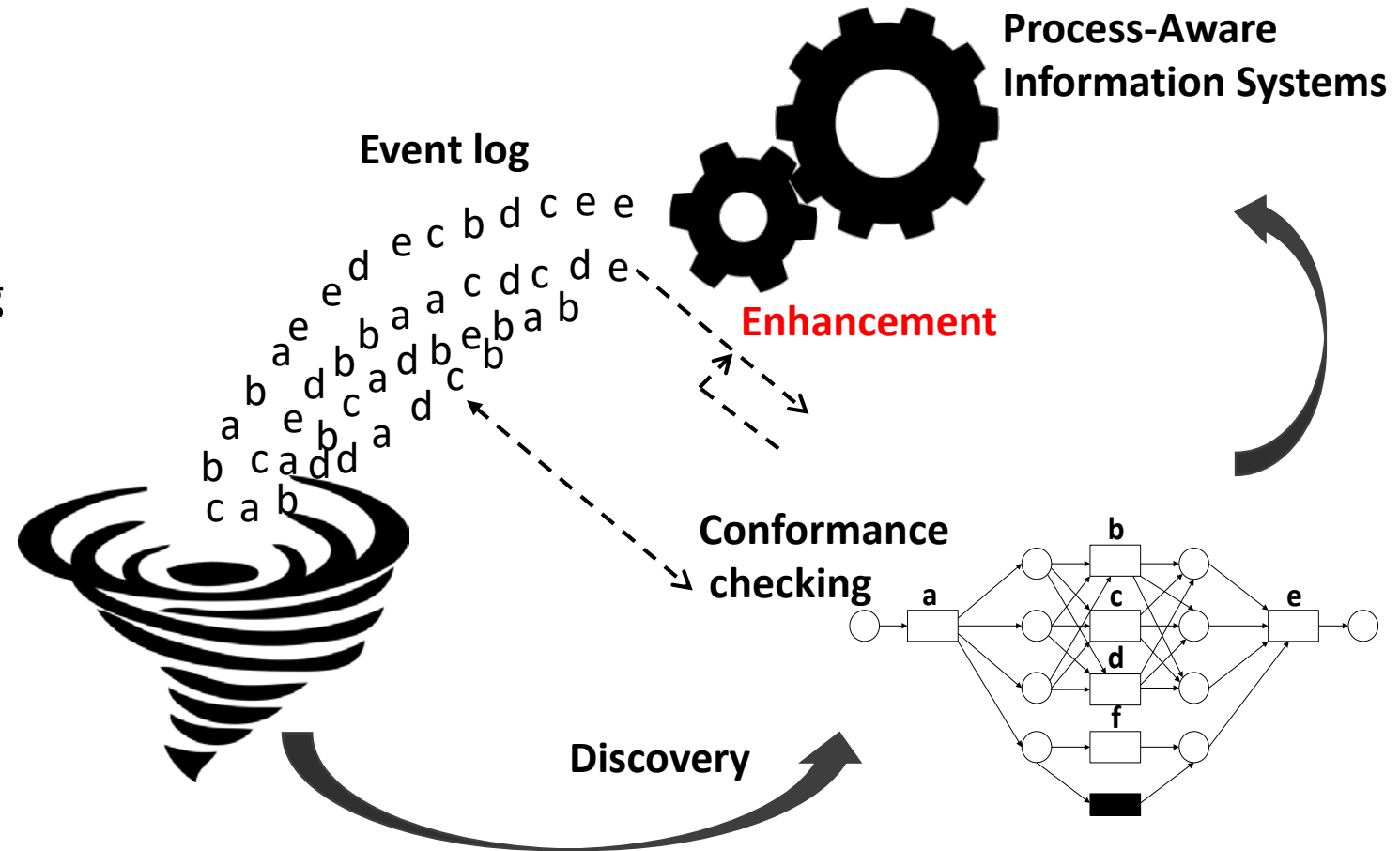


Some non-local dependencies may be lost.

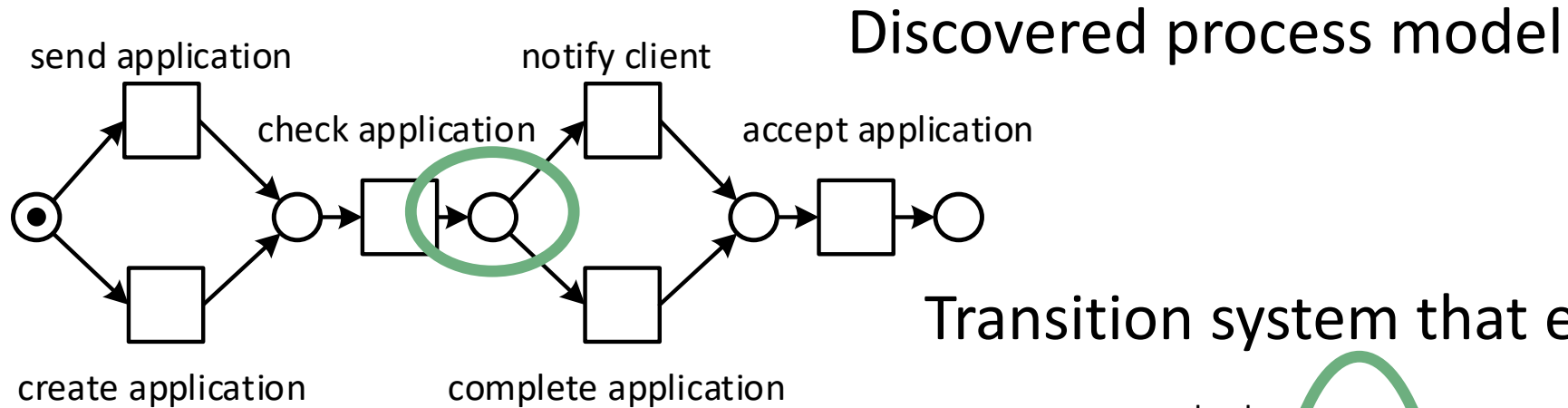


# Process mining

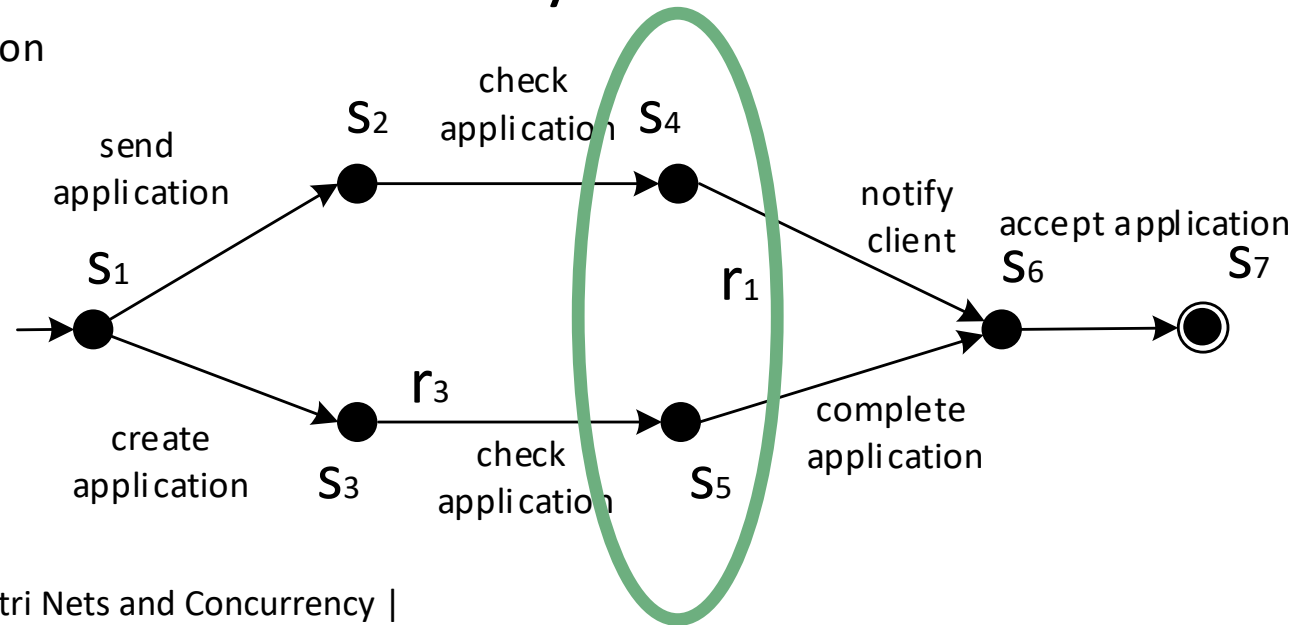
- Discovery
- Conformance checking
- **Enhancement**
  - **Repair**



# False Free-Choice Relation



Transition system that encodes event log L



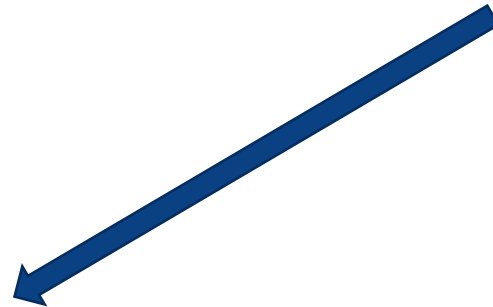
The local choice may depend on the process history

# Repair Using Non-Local Constraints

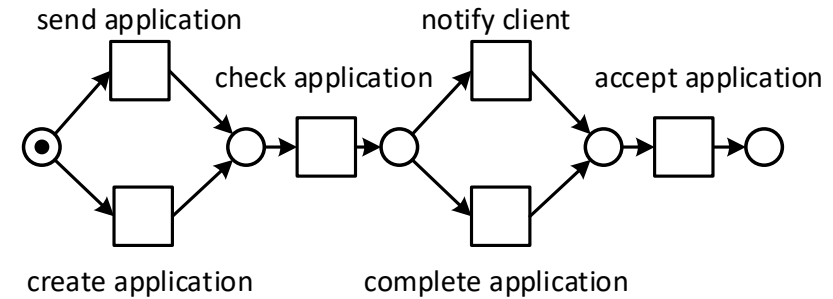
Event log

$$L = \{ \langle \text{send application}, \text{check application}, \text{notify client}, \text{accept application} \rangle, \langle \text{create application}, \text{check application}, \text{complete application}, \text{accept application} \rangle \}.$$

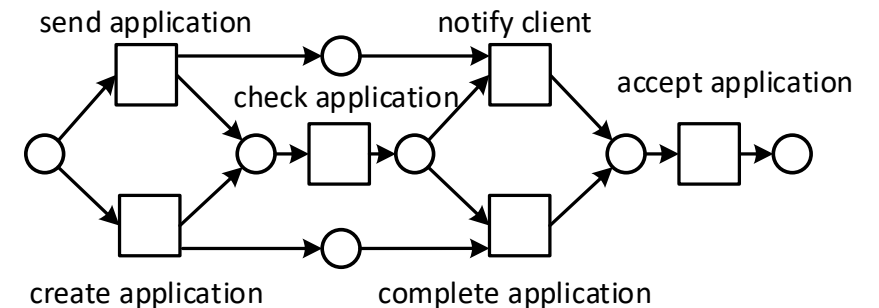

Non-local constraints



Free-choice process model



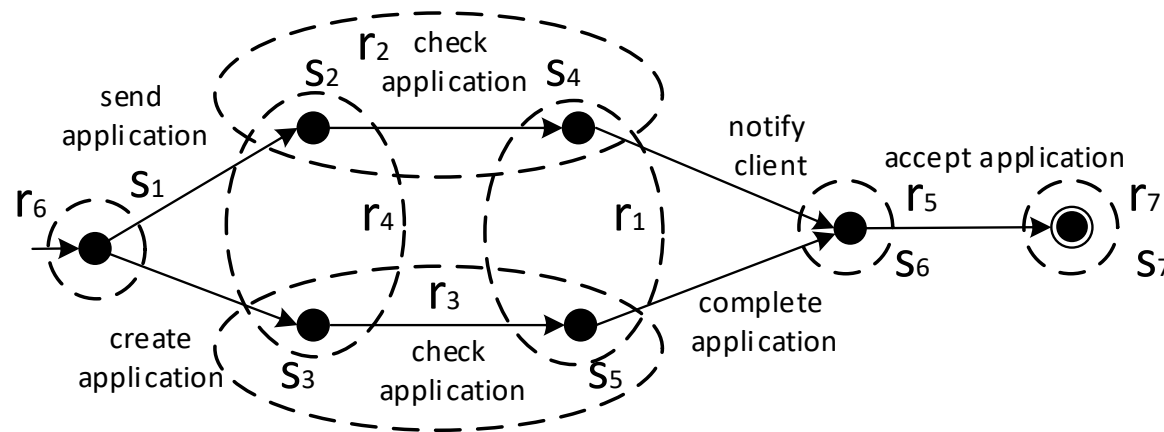
Process model with non-local constraints



# State-based Region Synthesis

Let  $TS = (S, E, T, s_i, S_f)$  be a transition system and  $r \subseteq S$  be a subset of states. Subset  $r$  is a **region** iff for each event  $e \in E$  one of the following conditions holds:

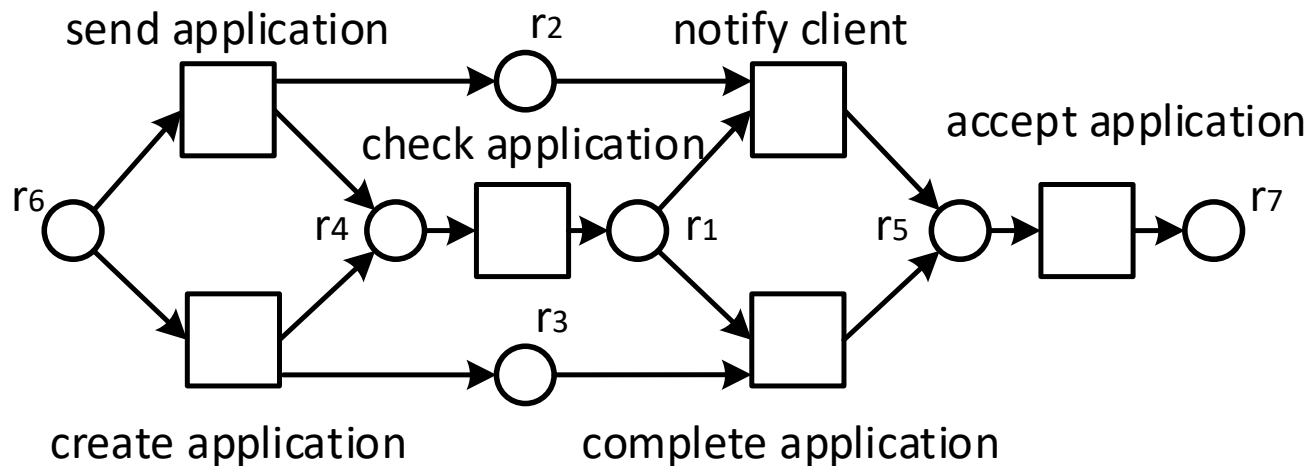
- all the transitions  $s_1 \xrightarrow{e} s_2$  **enter**  $r$ , i.e.,  $s_1 \notin r$  and  $s_2 \in r$ ,
- all the transitions  $s_1 \xrightarrow{e} s_2$  **exit**  $r$ , i.e.,  $s_1 \in r$  and  $s_2 \notin r$ ,
- all the transitions  $s_1 \xrightarrow{e} s_2$  **do not cross**  $r$ , i.e.,  $s_1, s_2 \in r$  or  $s_1, s_2 \notin r$ .



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# State-based Region Synthesis

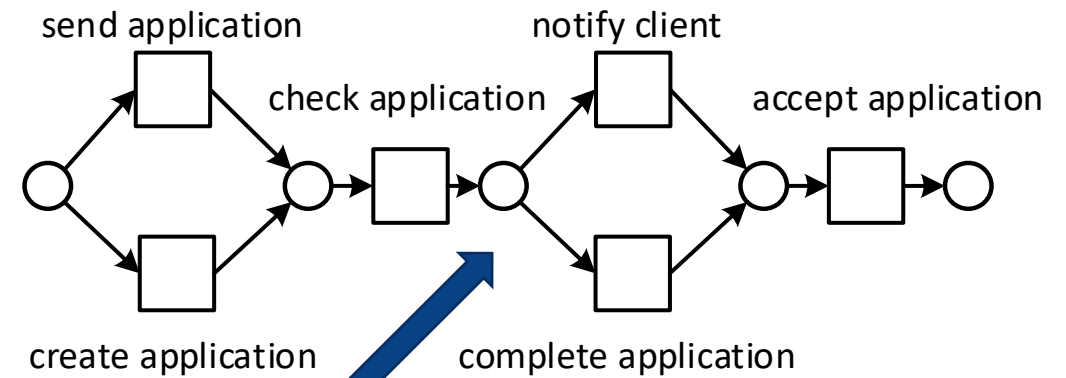
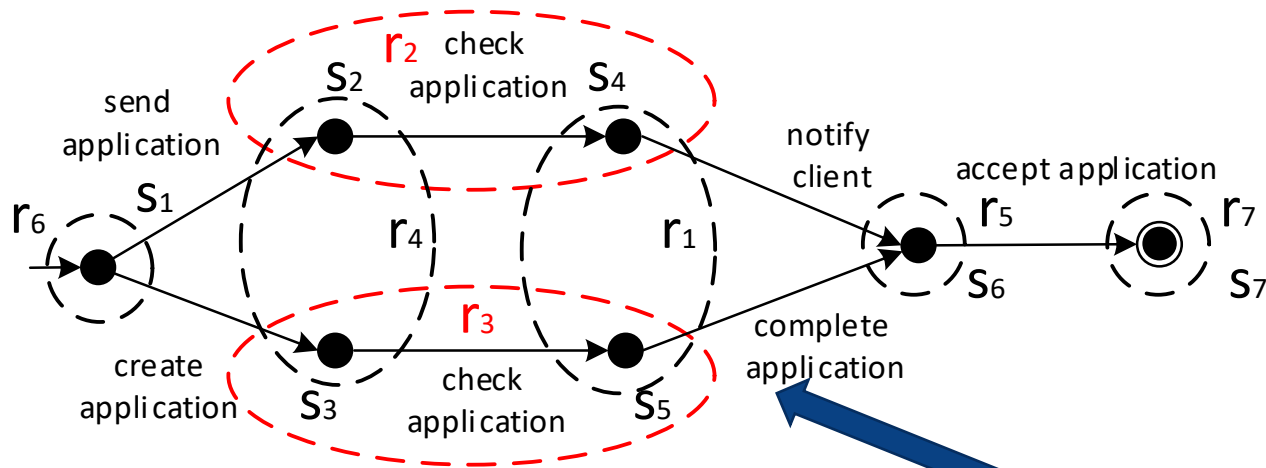
Region  $r$  separates two different states  $s, s' \in S$ ,  $s \neq s'$ , iff  $s \in r$  and  $s' \notin r$ . Finding such a region is the *state separation problem* between  $s$  and  $s'$  and is denoted by  $SSP(s, s')$ .

When an event  $e$  is not enabled in a state  $s$ , i.e.,  $s \not\rightarrow e$ , a region  $r$ , containing  $s$  may be found, such that  $e$  does not *exit*  $r$ . Finding such a region is known as the *event/state separation problem* between  $s$  and  $e$  and is denoted by  $ESSP(s, e)$ .

**Theorem.** A  $TS$  can be synthesized into a safe Petri net  $N$  such that the reachability graph of  $N$  is isomorphic to  $TS$  if all  $SSP$  and  $ESSP$  problems are solvable.

# State-based Region Synthesis

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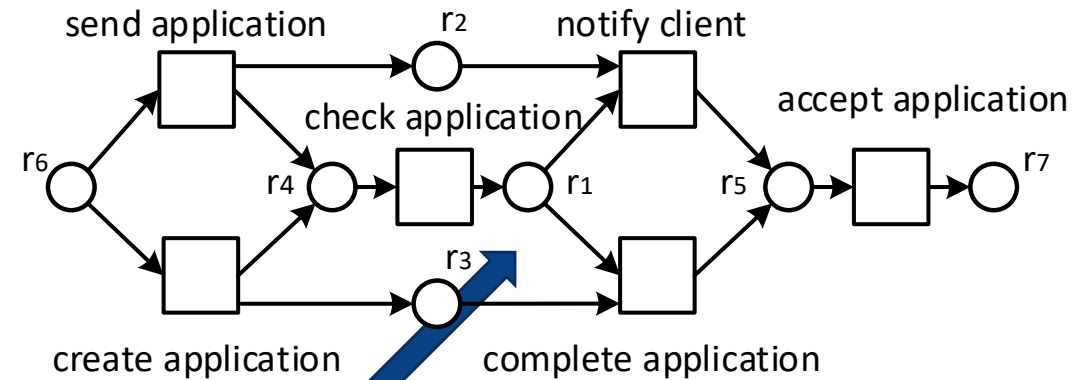
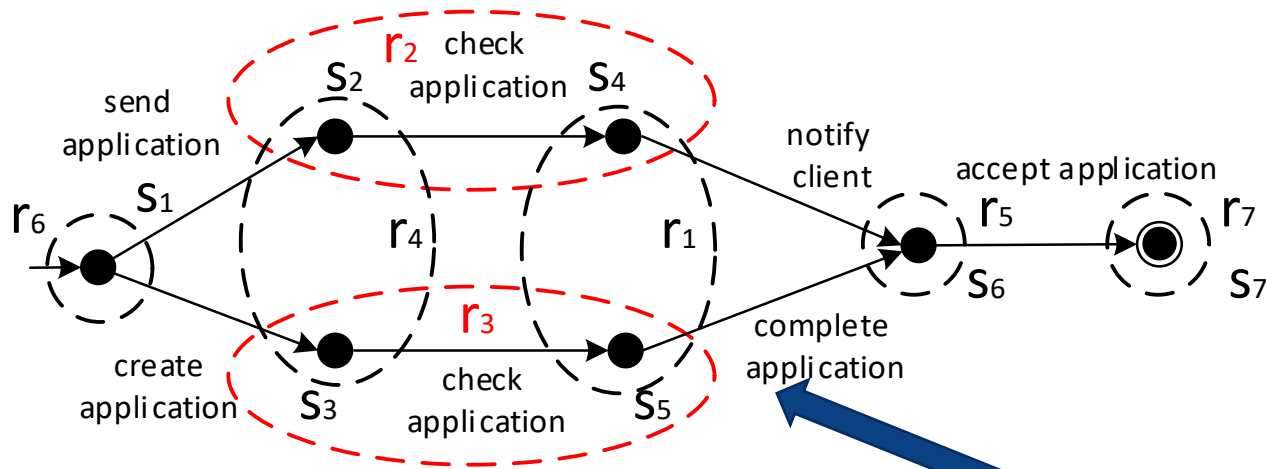
$ESSP(s_4, \text{"complete application"})?$

$ESSP(s_5, \text{"notify client"})?$

False free-choice relation

# State-based Region Synthesis

When an event  $e$  is not enabled in a state  $s$ , i.e.,  $s \not\rightarrow e$ , a region  $r$ , containing  $s$  may be found, such that  $e$  does not *exit*  $r$ . Finding such a region is known as the *event/state separation problem* between  $s$  and  $e$  and is denoted by  $ESSP(s, e)$ .



**ESSP( $s_4$ , "complete application")?**

**ESSP( $s_5$ , "notify client")?**

False free-choice relation



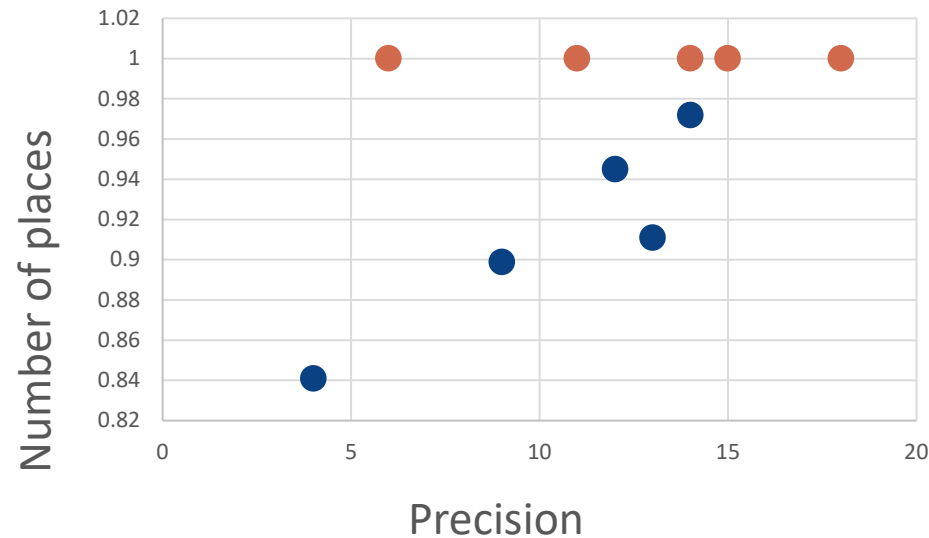


# Formal Properties of Repair Algorithm

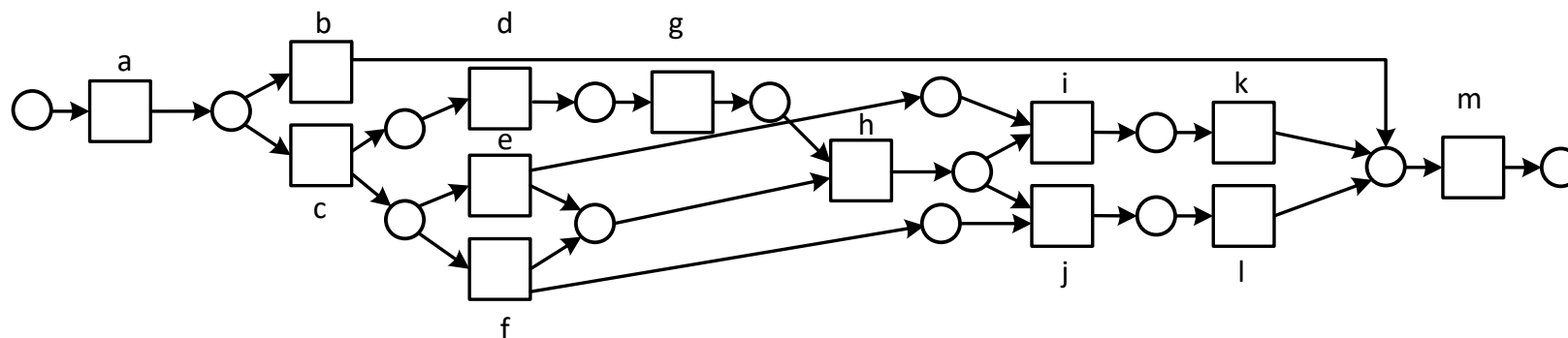
**Theorem (Fitness).** Let  $\sigma \in L$  be a trace of an event log  $L \in E^*$ , and  $N = (P, T, F, l)$ ,  $l : T \rightarrow E$  be a free-choice workflow net, such that its language contains  $\sigma$ , i.e.,  $\sigma \in \mathcal{L}(N)$ . Workflow net  $N' = (P \cup P', T, F', l)$ ,  $l : T \rightarrow E$ , is obtained from  $N$  and  $L$  using Repair algorithm. Then the language of  $N'$  contains  $\sigma$ , i.e.,  $\sigma \in \mathcal{L}(N')$ .

**Theorem (Precision).** Let  $N = (P, T, F, l)$ ,  $l : T \rightarrow E$ , be a free-choice workflow net and let  $L$  be an event log over set of events  $E$ . If workflow net  $N'$  is obtained from  $N$  and  $L$  by Repair algorithm, then the language of  $N$  contains the language of  $N'$ , i.e.,  $\mathcal{L}(N') \subseteq \mathcal{L}(N)$ .

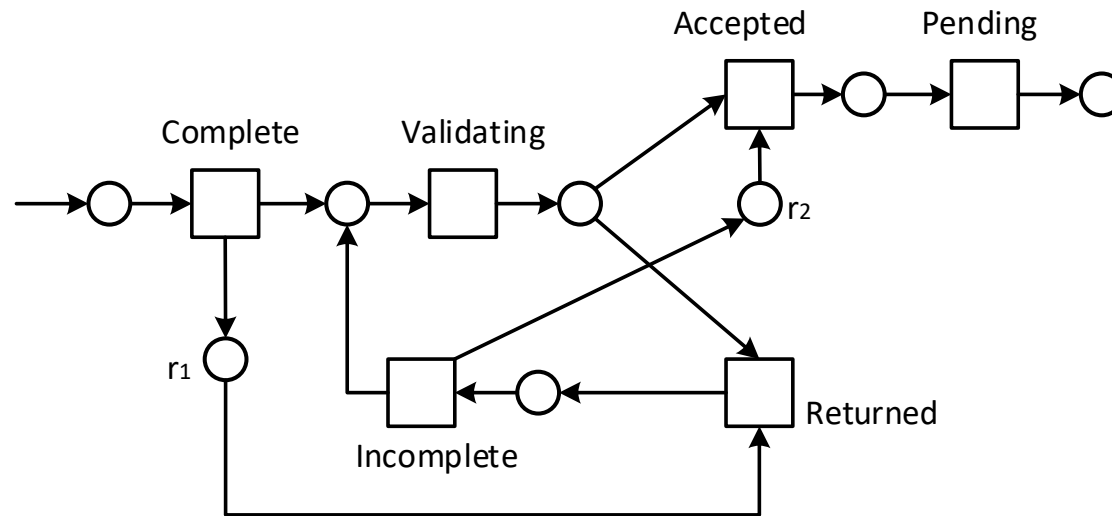
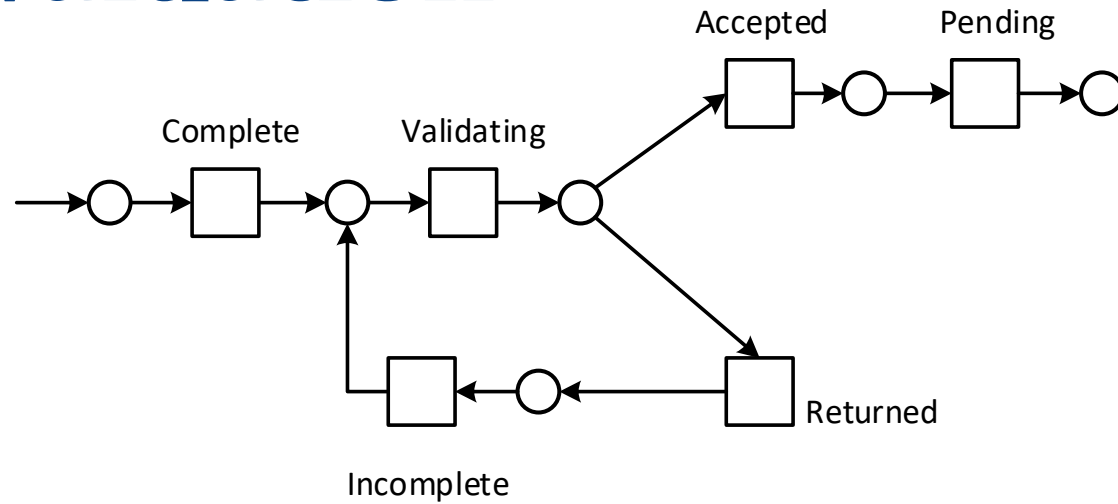
# Evaluation



The plugin is open-source and was implemented in Apromore Community Edition

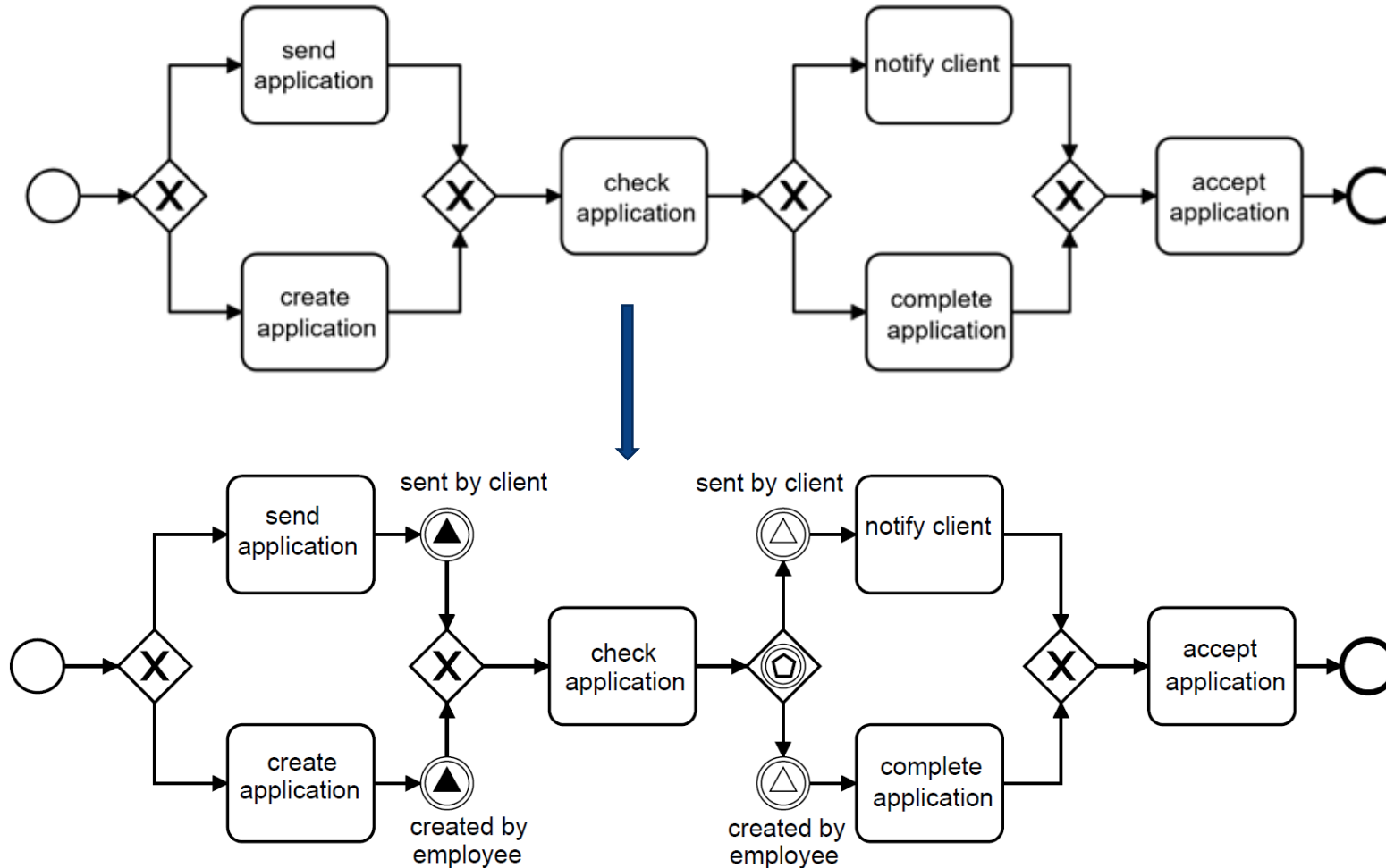


# Evaluation





# BPMN (Business Process Model and Notation)





# Conclusion and Future work

Although the Petri net synthesis problem is reduced (only some constraints are to be found), it still remains NP-complete.

Thus, an extension of the proposed algorithm is to be advised to improve its performance characteristics.



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**Thank you**

